

stars in the *Durchmusterung* with the following results, giving for comparison the magnitudes assigned to them in the *Durchmusterung* and in Carrington's Red Hill Catalogue:—

No. in B. D.	Mag. B. D.	Mag. Carrington.	Mag. Knott.
+8° 13	6·5	6·2	6·5
22	9·2	9·5	9·4
26	9·5		10·4
27	8·6	8·7	8·4
30	8·3	8·0	8·1
34	8·7	9·1	8·6

The star No. 26 does not appear to have been observed at Red Hill, and the magnitude estimate in the *Durchmusterung* seems to me to be rather too high.

I may note, in concluding, that the Variable was observed on three occasions at Red Hill in the year 1855, the dates of observation and corresponding magnitudes being December 19, 8·0; 21, 8·0; 30, 9·0. The star was probably near minimum at the last epoch.

*Knowles Loge, Cuckfield,
1880, November 11.*

On the Annual Parallax of the Star P III 242. By Robert S. Ball, LL.D., F.R.S., Royal Astronomer of Ireland.

In the *Monthly Notices* vol. xx. p. 8 is a paper by O. Struve "On a Star which would be suitable for a Parallax Series." The star in question is P III 242, and its position for 1879·0 is $\alpha=3^{\text{h}}\ 59^{\text{m}}\ 30^{\text{s}}$ and $\delta=+37^{\circ}\ 45'\cdot3$. Argelander in his Catalogue of 560 stars had pointed out that P III 242 probably formed a wide binary system with the next following star of his Catalogue 50 *Persei*, on account of the equality in direction and quantity of their proper motions.

Struve remarks also that P III 242 is a double star of Herschel's first class (No. 531 of O. Struve's Catalogue), the components being of 6-7th and 8-9th magnitudes respectively, and 3" or 4" distant. The physical connection of the two components of P III 242 appears to be established by their equal proper motions. A fourth star, Arg. zone +37°, No. 877 (Mag. 7-8) is south preceding P III 242 at a distance of nearly 4'. This star does not belong to the system formed by P III 242 and 50 *Persei*, for the changes in its position with respect to P III 242 correspond exactly to the proper motion of the latter. "This star, therefore," says Struve in conclusion, "would be a very qualified object of comparison for determining the relative parallax of P III 242, for which a considerable amount is indicated."

by the proper motion and by the probable physical connection with 50 *Persei* at 15' distance."

So far as I know, no measures have hitherto been published with the view of testing whether Struve's surmise as to the existence of a parallax for P III 242 could be substantiated. I therefore commenced a series of observations in January 1879 of the distance and position of the comparison star which Struve suggested from the larger star of the pair P III 242. The instrument employed was the South Equatoreal at Dunsink Observatory, with the Pistor and Martin filar micrometer. The methods of observation and of reduction are the same as those employed by Dr. Brunnow and myself in previous investigations. See Parts I., II., III. of the "Dunsink Observations."

In an important feature, however, the observations now to be discussed are very different from those which had previously been made with our micrometer. The distance in this case was no less than 237" \pm , which is greatly in excess of the distances measured in the regular series of parallax observations contained in our previous publications. Had there been any suitable comparison star nearer to P III 242 I should certainly have preferred it, for the distance 237" is too great to be measured by our micrometer with the accuracy which can be attained when the distance is only about one or two minutes. From this cause the results of the observations are not so satisfactory as I would wish, though they are quite sufficient to show that P III 242 has no large parallax.

The following are the observations which I have made of the distance and position, corrected for refraction and reduced to the mean places of the stars at the epoch 1879°:

Dist. and Pos. of A.Z. +37°, No. 877 from P III 242.

Date 1879.	Distance. "	Position. ° "
Jan. 11	237.558	207 17.35
Feb. 7	237.529	207 23.47
19	237.074	207 13.16
22	237.174	207 16.04
23	237.695	207 10.25
25	237.348	207 16.96
Mar. 1	237.220	207 9.08
19	237.605	207 15.99
Apr. 4	237.422	207 9.27
6		207 14.00
10	237.495	207 15.66
Aug. 14	237.268	207 19.18
22	236.973	207 8.47
23	237.177	207 12.83

Mr. Ball, On the Annual Parallax

XLII. I.

Date.	Distance.	Position.	
1879.			
Sept. 17	237°242	207°	16''28
Oct. 4	237°151	207°	20°24
5	237°203	207°	17°28
17	237°497	207°	16°14
25	237°315	207°	17°12
25	237°049	207°	22°83
Nov. 1	236°965	207°	8°40
2	237°305	207°	17°66
8	237°041	207°	19°72
8	237°423	207°	21°57
11	237°588	207°	12°86
Dec. 3	237°647	206°	59°53
5	237°186	207°	5°91
17	237°587	207°	25°42
18	237°215	207°	29°27
24	237°130	207°	22°88
1880.			
Jan. 9	236°715	207°	20°66

According to O. Struve (loc. cit.), the annual proper motion in right ascension is $+0^{\circ}0167$, and in declination $-0^{\circ}152$. It hence appears that the arc moved over in one year by P III 242 is $0''2497$, while the position angle of the star in the position it will occupy next year measured from the present position is $127^{\circ}5$. The correction to be applied to the observed distance in order to reduce the observed distance to that between the places at the epoch is $+0''04407$ per annum, while the corresponding correction to the observed position angle is $-3'565$, or in arc $-0''2457$.

The adopted mean distance at the epoch is $237''320$, and the adopted mean position is $207^{\circ}13'86$.

From the usual formulæ it is found that when \odot is the Sun's longitude, R the Sun's radius vector, and π the annual parallax of P III 242, the correction to be applied to the observed distance to clear it from the effects of parallax is (the figures in brackets denoting logarithms)

$$-[9.82787]\pi R \cos(\odot - 174^{\circ}56'0'')$$

while the corresponding correction of the observed position angle is

$$-[9.90007]\pi R \cos(\odot - 142^{\circ}8'29'').$$

Assuming that $-x$ is the correction to be applied to the

Nov. 1880.

of the Star P III 242.

39

assumed mean distance, while x' is the correction to the assumed value of the proper motion in distance, and κ is a possible difference in the coefficients of aberration of the two stars, then we have from the observations of the distance the following equations of condition :—

P III 242.

Equations of Condition, from Distance.

					Residuals.	Weight.
x	$+ .0274 x'$	$+ .2877 \pi$	$- .6038 \kappa$	$+ .239 = 0$	$+ .021$	
	$+ .1013$	$+ .5308$	$- .4011$	$+ .214 = 0$	$+ .052$	
	$+ .1342$	$+ .6034$	$- .2791$	$- .240 = 0$	$- .374$	$\frac{1}{2}$
	$+ .1424$	$+ .6175$	$- .2466$	$- .140 = 0$	$- .268$	
	$+ .1451$	$+ .6218$	$- .2357$	$+ .382 = 0$	$+ .257$	
	$+ .1506$	$+ .6299$	$- .2134$	$+ .035 = 0$	$- .086$	
	$+ .1615$	$+ .6438$	$- .1684$	$- .093 = 0$	$- .209$	
	$+ .2108$	$+ .6672$	$+ .0402$	$+ .294 = 0$	$+ .229$	
	$+ .2546$	$+ .6338$	$+ .2212$	$+ .113 = 0$	$+ .081$	
	$+ .2711$	$+ .6088$	$+ .2851$	$+ .187 = 0$	$+ .172$	
	$+ .6160$	$- .5645$	$+ .3734$	$- .025 = 0$	$+ .057$	$\frac{1}{2}$
	$+ .6379$	$- .6091$	$+ .2953$	$- .319 = 0$	$- .241$	$\frac{1}{2}$
	$+ .6407$	$- .6139$	$+ .2851$	$- .115 = 0$	$- .038$	
	$+ .7091$	$- .6739$	$+ .0113$	$- .047 = 0$	$.110.$	
	$+ .7557$	$- .6455$	$- .1825$	$- .136 = 0$	$- .089$	
	$+ .7584$	$- .6421$	$- .1935$	$- .083 = 0$	$- .038$	
	$+ .7913$	$- .5865$	$- .3217$	$+ .212 = 0$	$+ .249$	$\frac{1}{2}$
	$+ .8132$	$- .5352$	$- .4002$	$+ .031 = 0$	$+ .069$	
	$+ .8132$	$- .5352$	$- .4002$	$- .235 = 0$	$- .201$	
	$+ .8323$	$- .4818$	$- .4628$	$- .318 = 0$	$- .286$	
	$+ .8351$	$- .4736$	$- .4712$	$+ .022 = 0$	$+ .053$	
	$+ .8515$	$- .4214$	$- .5187$	$- .241 = 0$	$- .211$	
	$+ .8515$	$- .4214$	$- .5187$	$+ .141 = 0$	$+ .171$	
	$+ .8597$	$- .3935$	$- .5404$	$+ .306 = 0$	$+ .337$	
	$+ .9199$	$- .1611$	$- .6507$	$+ .368 = 0$	$+ .405$	
	$+ .9254$	$- .1384$	$- .6561$	$- .093 = 0$	$- .051$	
	$+ .9583$	$+ .0015$	$- .6709$	$+ .309 = 0$	$+ .357$	
	$+ .9610$	$+ .0133$	$- .6708$	$- .062 = 0$	$- .013$	
	$+ .9774$	$+ .0835$	$- .6655$	$- .147 = 0$	$.160.$	
	$+ 1.0219$	$+ .2699$	$- .6150$	$- .560 = 0$	$- .480$	

The normal equations deduced by the method of least squares, and making allowance for the weights, are :—

$$\begin{aligned}
 +28.000 & x + 17.039 & x' - 1.1059 & \pi - 8.6094 & \kappa + .18500 & = 0, \\
 +17.039 & x + 13.505 & x' - 4.1275 & \pi - 6.6243 & \kappa - .58021 & = 0, \\
 -1.1059 & x - 4.1275 & x' + 7.1845 & \pi + .77499 & \kappa + .85472 & = 0, \\
 -8.6094 & x - 6.6243 & x' + 7.7499 & \pi + 5.3655 & \kappa - .029128 & = 0.
 \end{aligned}$$

Solving these, we deduce

$$\begin{aligned}
 x &= -0.1459 \pm 0.08, \\
 x' &= +0.3009 \pm 0.15, \\
 \pi &= +0.0163 \pm 0.09, \\
 \kappa &= +0.1405 \pm 0.12.
 \end{aligned}$$

The sum of the squares of the residuals is 1.2732 , from which the probable error of one observation is $\pm 0''.15$. The sum of the squares of the absolute terms is 1.4638 .

We next proceed to form the equations of condition from the observations of the position angle. In a complete series of measures four observations of the parallel and four of the position angle have been made. Owing to the great distance of the stars, the measurements of the position angle (estimated in arc) are not very satisfactory, and on two occasions (Dec. 3 and Dec. 5, 1879) the discrepancies have attained to very undesirable dimensions. The residual on Dec. 3 is no less than $-1''.332$, but only a weight of $\frac{1}{2}$ attaches to this result, because it was based on but two observations of the parallel and two of the position. The notes at the time of observation are, "Snow and severe frost; low and hazy but tolerably steady." On the next night of observation, Dec. 5, the number of observations was complete, and they were fairly accordant; the notes at the time record, "Good definition; thaw; occasional clouds." The residual on this occasion is $-0''.895$. It will be noticed that these observations occur at dates when the parallax produces but very little effect, the coefficient being $+.2536$ on the first occasion, and $+.2801$ on the second.

The following are the equations of condition which are deduced from the position angle:—

P III 242.

Equations of Condition, from Position Angle.

				Residuals.	Weight.
x	$+ .0287 x'$	$+ .6715 \pi$	$- .4089 \kappa$	$+ .234 = 0$	$+ .103$
	$+ .1028$	$+ .7839$	$- .0470$	$+ .638 = 0$	$+ .544$
	$+ .1352$	$+ .7783$	$+ .1186$	$- .082 = 0$	$- .152 \quad \frac{1}{2}$
	$+ .1437$	$+ .7714$	$+ .1609$	$+ .115 = 0$	$+ .052$
	$+ .1465$	$+ .7686$	$+ .1752$	$- .286 = 0$	$- .343$

Nov. 1880.

of the Star P III 242.

41

					Residuals.	Weight.
+ .1518	x'	+ .7627	π	+ .2011	κ	+ .176 = 0
+ .1624		+ .7480		+ .2534		- .370 = 0
+ .2119		+ .6367		+ .4743		+ .095 = 0
+ .2558		+ .4856		+ .6308		- .380 = 0
+ .2613		+ .4639		+ .6471		- .055 = 0
+ .2723		+ .4189		+ .6774		+ .057 = 0
+ .6179		- .8058		+ .0053		+ .215 = 0
+ .6398		- .7980		- .1014		- .530 = 0
+ .6427		- .7959		- .1153		- .230 = 0
+ .7106		- .6747		- .4268		- .003 = 0
+ .7572		- .5207		- .6017		+ .254 = 0
+ .7599		- .5101		- .6106		+ .049 = 0
+ .7927		- .3731		- .7022		+ .038 = 0
+ .8141		- .2742		- .7465		+ .024 = 0
+ .8143		- .2735		- .7468		+ .419 = 0
+ .8335		- .1805		- .7748		- .582 = 0
+ .8364		- .1663		- .7780		- .056 = 0
+ .8522		- .0872		- .7910		+ .195 = 0
+ .8523		- .0865		- .7911		+ .322 = 0
+ .8609		- .0435		- .7947		- .281 = 0
+ .9205		+ .2536		- .7531		- .216 = 0
+ .9261		+ .2801		- .7434		- .777 = 0
+ .9598		+ .4318		- .6639		+ .562 = 0
+ .9624		+ .4427		- .6564		+ .827 = 0
+ .9789		+ .5091		- .6044		+ .381 = 0
+ 1.0233		+ .6155		- .4916		+ .217 = 0
						+ .090

The normal equations deduced from these by the method of least squares are, after making allowance for the weights :—

$$\begin{aligned}
 & + 27.250 \ x + 16.223 \ x' + 4.0258 \ \pi - 8.1716 \ \kappa + 1.0844 = 0, \\
 & + 16.223 \quad + 12.708 \quad - .1377 \quad - 8.3986 \quad + .77684 = 0, \\
 & + 4.0258 \quad - .1377 \quad + 8.5200 \quad + 1.6929 \quad + .85405 = 0, \\
 & - 8.1716 \quad - 8.3986 \quad + 1.6929 \quad + 8.6527 \quad - .78159 = 0.
 \end{aligned}$$

From which we obtain—

$$\begin{aligned}
 x &= + 0.0185 \pm 0.14, \\
 x' &= + 0.0076 \pm 0.27, \\
 \pi &= - 0.1371 \pm 0.11, \\
 \kappa &= + 0.1420 \pm 0.18.
 \end{aligned}$$